

Math 141.1 – Test I
Tuesday, Sept. 21, 1993

Name _____ **Show your work for full credit**

1. Let f be defined by

$$f(x) = \begin{cases} 5 - x^2, & \text{if } -1 < x < 1 \\ 2(2 - x), & \text{if } x \geq 1. \end{cases}$$

- (a) Sketch the graph of f .
(b) Determine the domain and range of f .
(c) Is f continuous at the points $x = -1, 0, 1$? Verify your answer.
2. Using the properties of limits, find the the following limits putting in each step:

(a) $\lim_{x \rightarrow 3} \frac{x^2 - 4x + 3}{x^2 - 9}$

(b) $\lim_{x \rightarrow 2} \frac{x^2 - 4x + 3}{x^2 - 9}$

(c) $\lim_{x \rightarrow 0} \frac{\tan(x)}{x \cos(x)}$

3. Using the definition of derivative and the properties of **limits**, compute the derivative of f at $x = 2$ where f is given by

$$f(x) = x^2 + x - 3.$$

4. Let

$$f(x) = 2x^3 - 6x - 2.$$

- (a) Compute the slope of the tangent line to the graph of f when $x = 1$.
(b) Give the equation of the tangent line to the graph of f at the same point.
(c) For which values of x is the tangent line horizontal?
5. Using the properties of **derivatives**, determine the derivatives of each of the following functions:
- (a) $g(x) = (2x^2 - 3)(1 - 2x + x^2)$
(b) $f(x) = x^2 e^x - 2x^3$ (Hint: You can use $D_x(e^x) = e^x$)

6. **[EXTRA CREDIT]**

Using the definition of 'limit', prove that

$$\lim_{x \rightarrow 0} x^2 = 0.$$