

Exam 1  
February 20, 2001

Name: \_\_\_\_\_  
SS #: \_\_\_\_\_

Instructions:

1. There are a total of 7 problems on 8 pages. Check that your copy of the exam has all of the problems.
2. You must show all of your work to receive credit for a correct answer.
3. Your answers must be written legibly in the space provided. You may use the back of a page for additional space; please indicate clearly when you do so.

Problem	Points	Score
1	15	
2	15	
3	15	
4	20	
5	8	
6	15	
7	12	
Total	100	

Good Luck!

1. (15 points) Let  $\mathbf{a} = 2\mathbf{i} - 5\mathbf{j} - \mathbf{k}$ ,  $\mathbf{b} = 3\mathbf{i} - \mathbf{j}$ , and  $\mathbf{c} = \langle 1, 0, -6 \rangle$ . Find each of the following:

(a)  $\mathbf{a} \cdot \mathbf{c}$

(b)  $\mathbf{b} \times \mathbf{c}$

(c)  $\mathbf{c} \cdot \mathbf{c} - |\mathbf{c}|$

2. (15 points) Let  $C$  be the parametric curve  $x = t$ ,  $y = t^2$ ,  $z = 3$ .

(a) Find all points on the curve with  $y = 4$ .

(b) Find the tangent line to the curve at the point  $(-1, 1, 3)$ .

(c) Find the equation of the normal plane to the curve at the point  $(-1, 1, 3)$ .

(d) Find the speed of a particle that follows this curve.

(e) Find all points where the particle's speed is zero. Explain your answer.

3. (15 points)

(a) What is the direction of the line  $x = -3 + 2t$ ,  $y = 3$ ,  $z = -1 + 2t$ ?

(b) Find parametric equations for the line through  $(6, 1, -3)$  and  $(-2, 1, 3)$ .

(c) Find the center and radius of the sphere with equation  $x^2 + y^2 + z^2 + 6x - 2y + 5 = 0$ .

4. (20 points) Consider the curve  $\mathbf{r}(t) = e^t \sin t \mathbf{i} + e^t \cos t \mathbf{j} + e^t \mathbf{k}$ ,  $1 \leq t \leq 5$ . Find each of the following:

(a)  $\mathbf{r}'(\pi)$

(b)  $\mathbf{T}(\pi)$

(c)  $\mathbf{r}''(\pi)$

(d) the length of the curve

5. (8 points) Find all unit vectors that are perpendicular to both of the vectors  $\mathbf{a} = 3\mathbf{i} - 3\mathbf{j} + \mathbf{k}$  and  $\mathbf{b} = -\mathbf{i} - 2\mathbf{j} + 4\mathbf{k}$ .

6. (15 points) Sketch the level curves of  $f(x, y) = x^2 + y^2$  for  $k = -1, 0, 1, 4, 9$ .  
*Remember to label the curves and the axes.*

7. (12 points) Let  $f(x, y) = 3x^2y^4 + 7\frac{x^2}{y^3}$ . Find

(a)  $\frac{\partial f}{\partial x}$

(b)  $\frac{\partial^2 f}{\partial x^2}$

(c)  $f_{xy}$