

Test #2, Math 115

Oct 17th, 2006

Name: _____

Direction: Please *print* your name. And show your work for credit. No work=No credit.

1. Solve the following quadratic equation use any way you like. (10 points)

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{8 \pm \sqrt{64 - 4 \times 2 \times 3}}{2 \times 2}$$

$$= \frac{8 \pm \sqrt{40}}{4} = \frac{8 \pm 2\sqrt{10}}{4} = \frac{4 \pm \sqrt{10}}{2}$$

$2x^2 - 8x + 3 = 0$ or $2(x^2 - 4x) + 3$

$$2(x^2 - 4x + 4) - 8 + 3 = 0$$

$$2(x^2 - 4x + 4) = 5$$

$$2(x-2)^2 = 5$$

$$(x-2)^2 = \frac{5}{2}$$

$$x-2 = \pm \sqrt{\frac{5}{2}}$$

$$x = 2 \pm \frac{\sqrt{10}}{2}$$

2. Solve the following equation use any way you like. (10 points)

$$\sqrt{x-4} + x = 4$$

$$\sqrt{x-4} = -x+4$$

$$x-4 = (4-x)^2$$

$$x-4 = 16 - 8x + x^2$$

$$x^2 - 9x - 20 = 0 \Rightarrow (x-4)(x-5) = 0$$

3. For the following equation of a circle find the center and the radius. (10 points)

$$x^2 + 2x + y^2 - 4y + 2 = 0$$

$$(x^2 + 2x + 1) + (y^2 - 4y + 4) + 2 = 1 + 4$$

$$(x+1)^2 + (y-2)^2 = 3$$

$$(x+1)^2 + (y-2)^2 = (\sqrt{3})^2$$

center : (-1, 2)

radius : $\sqrt{3}$

$x=4$ or $x=5$
 plug in and check
 only $x=4$ is a solution.

4. Find the equation of the straight line that passes (1, 2) and perpendicular to $2y - x = 4$. (10 points)

$$2y - x = 4 \Rightarrow 2y = x + 4 \Rightarrow y = \frac{1}{2}x + 2, m = \frac{1}{2}$$

So $m' = -2$

$$(y - 2) = m'(x - 1)$$

$$y - 2 = -2(x - 1)$$

$$y = -2x + 4$$

5. Find the equation of the straight line that passes (1, 1) and (4, 3). Show your answer in the "slope-intercept" form. (10 points)

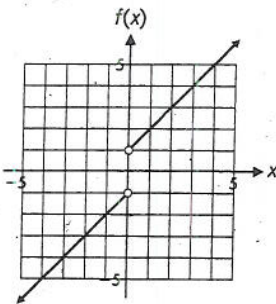
$$m = \frac{3 - 1}{4 - 1} = \frac{2}{3}$$

$$(y - 1) = \frac{2}{3}(x - 1)$$

$$(y - 1) = \frac{2}{3}x - \frac{2}{3}$$

$$y = \frac{2}{3}x + \frac{1}{3}$$

6. For the following graph of function find the domain and the range. (10 points)



Domain: $(-\infty, 0) \cup (0, \infty)$

Range: $(-\infty, -1) \cup (1, \infty)$

7. For the quadratic function $f(x) = -2x^2 + 12x - 20$, find the vertex, axis and sketch the graph. (10 points)

$$f(x) = -2(x^2 - 6x) - 20$$

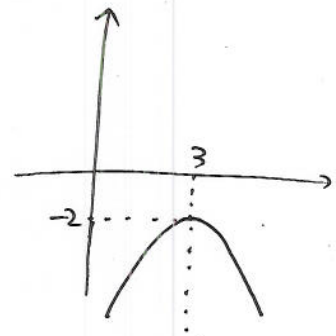
$$= -2(x^2 - 6x + 9 - 9) - 20$$

$$= -2(x - 3)^2 + 18 - 20$$

$$= -2(x - 3)^2 - 2$$

Vertex $(3, -2)$

axis: $x = 3$



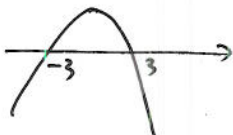
8. For $f(x) = \sqrt{36 - x^2}$ and $g(x) = 2x$, find $(f \circ g)(x)$ and its domain. (10 points for $(f \circ g)$, 10 points for domain)
Hint: Solve a quadratic inequality to find the domain.

$$(f \circ g)(x) = f(g(x)) = \sqrt{36 - (2x)^2} = \sqrt{36 - 4x^2}$$

Domain: $36 - 4x^2 \geq 0$

$$-4(x-3)(x+3) \geq 0 \quad \text{intercepts: } \{3, -3\}$$

$$\Rightarrow -3 \leq x \leq 3$$



Hence, domain of $f \circ g$ is $-3 \leq x \leq 3$
or $[-3, 3]$

9. Divide, using long division or synthetic division. Indicate the quotient and the remainder. (10 points)

$$(3x^3 + 2x^2 + 20) \div (x + 2)$$

$$\begin{array}{r} 3x^2 - 4x + 8 \\ x+2 \overline{) 3x^3 + 2x^2 + 0x + 20} \\ \underline{3x^3 + 6x^2} \\ -4x^2 + 0x \\ \underline{-4x^2 - 8x} \\ 8x + 20 \\ \underline{8x + 16} \\ 4 \end{array}$$

Quotient: $3x^2 - 4x + 8$

Remainder: 4

$$x+2 = x-r \Rightarrow r = -2$$

$$\begin{array}{r} 3 \quad 2 \quad 0 \quad 20 \\ -2 \overline{) 3 \quad -4 \quad 8 \quad 4} \\ \underline{-6 \quad 8 \quad -16} \\ 3 \quad -4 \quad 8 \quad 4 \\ \underline{-6 \quad 8 \quad -16} \\ 3 \quad -4 \quad 8 \quad 4 \\ \underline{-6 \quad 8 \quad -16} \\ 3 \quad -4 \quad 8 \quad 4 \\ \underline{-6 \quad 8 \quad -16} \\ 3 \quad -4 \quad 8 \quad 4 \end{array}$$

Quotient remainder

Quotient: $3x^2 - 4x + 8$

Remainder: 4