## Homework 5

Due at the beginning of class on Wednesday, March 18.
(17) Fix a degree $d$. Let $\phi: \mathbb{A}^{2} \rightarrow \mathbb{A}^{3}$ be the morphism

$$
\phi\left(x_{1}, x_{2}\right)=\left(x_{1}^{d}, x_{1} x_{2}^{d-1}, x_{2}^{d}\right) .
$$

Find $I(\operatorname{im} \phi)$.
(18) Let $X$ be the generic $2 \times 3$ matrix, $\Delta_{1}, \Delta_{2}, \Delta_{3}$ be the three $2 \times 2$ minors of $X$, and $\phi: \mathbb{A}^{6} \rightarrow \mathbb{A}^{3}$ be the morphism

$$
\phi(p)=\left(\Delta_{1}(p), \Delta_{2}(p), \Delta_{3}(p)\right) .
$$

Find $I(\operatorname{im} \phi)$.
(19) Hassett page 56, problem 3.25.
(20) Hassett page 69, problem 4.4.

