

Use the paper provided. Put your name on the front of the first page and the back of the last page. Each problem is worth 10 points. **NO CALCULATORS!**

1. Compute  $\iint_D \left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 dx dy$ , where  $D$  is the region inside

$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1.$$

2. Find the volume of the solid below  $x^2 + y^2 + z^2 = 1$  and above  $z = \sqrt{x^2 + y^2}$ .

3. Compute  $\iint_D (x+y)^3 e^{x-y} dx dy$ , where  $D$  is the region bounded by  $x+y = 1$ ,  $x+y = 5$ ,  $x-y = -1$ , and  $x-y = 2$ .

4. Compute  $\iint_D e^{x^2+y^2} dx dy$ , where  $D$  is the region inside  $x^2 + y^2 = 1$ .

5. Let  $D^*$  be the parallelogram with vertices at  $(-1, 3)$ ,  $(0, 0)$ ,  $(2, -1)$ , and  $(1, 2)$ , let  $D$  be the rectangle  $D = [0, 1] \times [0, 1]$ . Find a transformation  $T$  such that  $D$  is the image set of  $D^*$  under  $T$ .