

PRINT Your Name: \_\_\_\_\_

**Quiz for February 11, 2010**

The quiz is worth 5 points. **Remove EVERYTHING from your desk except this quiz and a pen or pencil.**

True or False. If true, prove it. If false, give a counter example. Let  $G$  be a group and let  $H$  be the subset  $H = \{g \in G \mid g^2 = \text{id}\}$ . Then  $H$  is a subgroup of  $G$ .

**ANSWER:** FALSE. Let  $G = D_3$ . We have  $H = \{\text{id}, \sigma, \sigma\rho, \sigma\rho^2\}$ . The set  $H$  is not a group because this set is not closed since  $\sigma$  and  $\sigma\rho$  are in  $H$  but the product  $\sigma(\sigma\rho) = \rho$  is not in  $H$ .