

9. Give an example of a non-cyclic ~~non~~<sup>abelian</sup> group of order 16. I do not need to see many details.

$\mathbb{Z}_2 \times D_4$  has order 16 and is not abelian

10. Find all of the subgroups of  $(\mathbb{Z}_{12}, +)$ . Be sure to tell me why you know that you have all of the subgroups.

$\mathbb{Z}_{12}$  is cyclic. Thus every subgroup is cyclic. The subgroups are

$$\langle [0]_{12} \rangle = \{[0]_{12}\}$$

$$\langle [1]_{12} \rangle = \langle [5]_{12} \rangle = \langle [7]_{12} \rangle = \langle [11]_{12} \rangle = \mathbb{Z}_{12}$$

$$\langle [2]_{12} \rangle = \langle [10]_{12} \rangle = \{[2]_{12}, [4]_{12}, [6]_{12}, [8]_{12}, [10]_{12}, [0]_{12}\}$$

$$\langle [3]_{12} \rangle = \langle [9]_{12} \rangle = \{[3]_{12}, [6]_{12}, [9]_{12}, [0]_{12}\}$$

$$\langle [4]_{12} \rangle = \langle [8]_{12} \rangle = \{[4]_{12}, [8]_{12}, [0]_{12}\}$$

$$\langle [6]_{12} \rangle = \{[6]_{12}, [0]_{12}\}$$