

9. Give an example of a group  $G$  and elements  $a$  and  $b$  of  $G$  with  $(ab)^3 \neq a^3b^3$ .  
Explain.

Let  $a = \sigma$  and  $b = \rho$  in  $G = D_3$ .

Observe that  $(ab)^3 = (\sigma\rho)^3 = \sigma\rho$

But  $a^3b^3 = \sigma^3\rho^3 = \sigma$   $\leftarrow \uparrow$   
we are not equal.

10. The group  $D_4$  has three ~~distinct~~ <sup>distinct</sup> subgroups of order 4. List the elements of each of these subgroups. (I do not need to see any details.)

$$\{e, \rho, \rho^2, \rho^3\}$$

$$\{e, \rho^2, \sigma\rho^2, \sigma\}$$

$$\{e, \rho^2, \sigma\rho, \sigma\rho^3\}$$