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## Quiz for September 4, 2009

True or False. (If True, prove it. If False, give a counterexample.) If $A$ and $B$ are $2 \times 2$ matrices with $A$ not the zero matrix and $A^{2}=A B$, then $A$ must equal $B$.
ANSWER: FALSE. Let $A=\left[\begin{array}{ll}1 & 1 \\ 1 & 1\end{array}\right]$ and $B=\left[\begin{array}{ll}2 & 0 \\ 0 & 2\end{array}\right]$. We see that $A$ is not the zero matrix, $A^{2}=A B=\left[\begin{array}{ll}2 & 2 \\ 2 & 2\end{array}\right]$, but $A \neq B$.

