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## Quiz for May 31, 2005

Find all values $a$ for which the system

$$
\begin{aligned}
x_{1}+2 x_{2} & =-3 \\
a x_{1}-2 x_{2} & =5
\end{aligned}
$$

has no solution. Explain thoroughly.
ANSWER: We apply the technique of Guassain Elimination to

$$
\left[\begin{array}{cc|c}
1 & 2 & -3 \\
a & -2 & 5
\end{array}\right]
$$

Replace $R_{2} \mapsto R_{2}-a R_{1}$ to get:

$$
\left[\begin{array}{cc|c}
1 & 2 & -3 \\
0 & -2-2 a & 5+3 a
\end{array}\right]
$$

If $-2-2 a \neq 0$, then the system of equations has exactly one solution. If $-2-2 a=0$ and $5+3 a=0$ (this never happens), then the system of equations has infinitely many solutions. If $-2-2 a=0$ and $5+3 a \neq 0$, then the system of equations has no solution. We conclude that:

If $a=-1$, then the system has no solutuion. Otherwise, the system of equations has a unique solution.

