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## Quiz for May 31, 2005

Find all values a for which the system

$$\begin{array}{rcl}
x_1 + 2x_2 &= -3 \\
ax_1 - 2x_2 &= 5
\end{array}$$

has no solution. Explain thoroughly.

**ANSWER:** We apply the technique of Guassain Elimination to

$$\begin{bmatrix} 1 & 2 & | & -3 \\ a & -2 & | & 5 \end{bmatrix}$$

Replace  $R_2 \mapsto R_2 - aR_1$  to get:

$$\begin{bmatrix} 1 & 2 & & -3 \\ 0 & -2 - 2a & & 5 + 3a \end{bmatrix}$$

If  $-2-2a \neq 0$ , then the system of equations has exactly one solution. If -2-2a = 0and 5+3a = 0 (this never happens), then the system of equations has infinitely many solutions. If -2-2a = 0 and  $5+3a \neq 0$ , then the system of equations has no solution. We conclude that:

> If a = -1, then the system has no solution. Otherwise, the system of equations has a unique solution.