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Quiz for November 1, 2005
Let $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ be the function which fixes the origin and rotates the plane by the angle $\theta=\frac{\pi}{3}$. Find a matrix $M$ with $T(v)=M v$ for all vectors $v$ in $\mathbb{R}^{2}$.

ANSWER: We saw in class that

$$
M=\left[\begin{array}{cc}
\cos \frac{\pi}{3} & -\sin \frac{\pi}{3} \\
\sin \frac{\pi}{3} & \cos \frac{\pi}{3}
\end{array}\right]=\left[\begin{array}{cc}
\frac{1}{2} & -\frac{\sqrt{3}}{2} \\
\frac{\sqrt{3}}{2} & \frac{1}{2}
\end{array}\right] .
$$

