

5. Define "linear combination". Use complete sentences.

Let v_1, v_2, \dots, v_p be vectors in \mathbb{R}^n . The vector v is a linear combination of v_1, \dots, v_p if there exist numbers c_1, \dots, c_p with

$$v = \sum_{i=1}^p c_i v_i$$

6. Define "linearly independent". Use complete sentences.

Let v_1, \dots, v_p be vectors in \mathbb{R}^n . The vectors v_1, \dots, v_p are linearly independent if the ~~only~~ numbers c_1, \dots, c_p with $\sum_{i=1}^p c_i v_i = 0$ are $c_1 = c_2 = \dots = c_p = 0$.

7. Define "linear transformation". Use complete sentences.

The function $T: \mathbb{R}^n \rightarrow \mathbb{R}^m$ is a linear transformation

iff

a) $T(u+v) = T(u) + T(v)$ for all u and v in \mathbb{R}^n

b) $T(cu) = cT(u)$ for all $u \in \mathbb{R}^n$ and $c \in \mathbb{R}$.