

Math 241, Spring 2001, Final Exam

PRINT Your Name: _____

Get your course grade from **TIPS/VIP** late on Thursday or later.

There are 19 problems on 10 pages. Problems 1 and 2 are worth 7 points each. Each of the other problems is worth 8 points. The exam is worth a total of 150 points. SHOW your work. **CIRCLE** your answer. **NO CALCULATORS!**

- (There is no partial credit for this problem. Make sure your answer is correct.)** Find the equation of the plane through $(1, 1, 1)$, $(1, 2, -2)$, and $(3, 1, -3)$.
- (There is no partial credit for this problem. Make sure your answer is correct.)** Find the equations of the line through $(1, 3, 4)$ and $(3, 6, 9)$.
- Graph and name $y^2 - x^2 = 1$ in 2-space.
- Graph and name $\frac{z^2}{16} - \frac{y^2}{9} + \frac{x^2}{25} = 1$ in 3-space.
- What are the equations of the line tangent to the curve which is parameterized by $\vec{r}(t) = (3t^3 + 2t)\vec{i} + 6t^2\vec{j} + 4t^3\vec{k}$ at $t = 1$?
- Find the equation of the plane tangent to the surface $z = x^2 + 3y^3$ at the point where $x = 3$ and $y = -1$.
- (There is no partial credit for this problem. Make sure your answer is correct.)** Let $\vec{a} = 2\vec{i} + 4\vec{j} + 6\vec{k}$ and $\vec{b} = 3\vec{i} + 4\vec{j} + \vec{k}$. Find vectors \vec{u} and \vec{v} with $\vec{b} = \vec{u} + \vec{v}$, \vec{u} parallel to \vec{a} , and \vec{v} perpendicular to \vec{a} .
- Find the point on $2x + 3y + 4z = 49$ which is closest to $(1, 2, 3)$.
- Where do the following two lines intersect? CHECK YOUR ANSWER!

$$\frac{x-1}{1} = \frac{y-8}{2} = \frac{z-8}{3} \quad \text{and} \quad \frac{x+4}{-1} = \frac{y-10}{2} = \frac{z+4}{-2}$$

- Find the length of the curve $\vec{r}(t) = t^2\vec{i} + t^3\vec{j}$ for $1 \leq t \leq 2$.
- Find the directional derivative of $f(x, y) = y^3 \ln x$ at the point $(1, 2)$ in the direction of $\vec{u} = \frac{1}{\sqrt{2}}(\vec{i} - \vec{j})$.
- Find all local maximum points, all local minimum points, and all saddle points of $f(x, y) = x^3 + y^3 - 6xy$.
- The temperature of a plate at the point (x, y) is $T(x, y) = 20 - 3x^2 - 2y^2$. Find the path that a heat seeking particle would travel if it starts at the point $(1, 4)$. (The particle always moves in the direction of the greatest increase in temperature.)