## Math 174, Fall 2003, Solution to Quiz 1

Question: Are $(p \wedge q) \vee r$ and $p \wedge(q \vee r)$ logically equivalent? Justify your answer. (You will probably want to use a truth table or well known logical equivalences.)
Answer: Here is the truth table:

| $p$ | $q$ | $r$ | $(p \wedge q) \vee r$ | $p \wedge(q \vee r)$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $T$ | $T$ | $T$ | $T$ | $T$ |  |
| $T$ | $T$ | $F$ | $T$ | $T$ |  |
| $T$ | $F$ | $T$ | $T$ | $T$ |  |
| $T$ | $F$ | $F$ | $F$ | $F$ |  |
| $F$ | $T$ | $T$ | $T$ | $F$ | $\star$ |
| $F$ | $T$ | $F$ | $F$ | $F$ |  |
| $F$ | $F$ | $T$ | $T$ | $F$ | $\star$ |
| $F$ | $F$ | $F$ | $F$ | $F$ |  |

The rows with $\star$ show that $(p \wedge q) \vee r$ and $p \wedge(q \vee r)$ are NOT logically equivalent.

