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Quiz for September 15, 2005

Find $\lim_{x \rightarrow 0^-} (1 - 2x)^{\frac{3}{x}}$. Explain carefully which facts you are using.

ANSWER: Let $t = \frac{-1}{x}$. The problem is equal to

$$\lim_{t \rightarrow +\infty} \left(1 + \frac{2}{t}\right)^{-3t} = \left(\lim_{t \rightarrow +\infty} \left(1 + \frac{2}{t}\right)^t\right)^{-3}.$$

We saw in class that $\lim_{t \rightarrow \infty} \left(1 + \frac{r}{t}\right)^t = e^r$. The answer to our problem is

$$(e^2)^{-3} = \boxed{e^{-6}}.$$