

Quiz #5

Name: _____

Key*You must show your work to get full credit.*

Part of the point of this quiz is to show how fast exponential functions grow.

Under ideal conditions the bacterium *E. coli* will double every $1/3$ hour. A single *E. coli* weighs 10^{-15} kg.

1. We start a colony *E. coli* with a single *E. coli*. Assuming that the weight of the colony doubles every $1/3$ hour, give a formula for the weight, $W(t)$, of the colony after t hours.

$$W(t) = W_0 \lambda^t = 10^{-15} \lambda^t$$

This doubles every $1/3$ hour, so

$$W(1/3) = 10^{-15} \lambda^{1/3} = 2 \cdot 10^{-15}$$

$$\lambda^{1/3} = 2$$

$$\lambda = (\lambda^{1/3})^3 = 2^3 = 8$$

$$W(t) = \frac{10^{-15} 8^t}{}$$

$$W(t) = 10^{-15} e^{2.079 t}$$

is also correct

2. The weight of the Earth is 6.0×10^{24} kg. How long does it take for our colony of *E. coli* to have the same weight as the Earth?

Time to reach mass of Earth is 44.05 hours.

We want to solve

$$W(t) = 10^{-15} 8^t = 6.0 \times 10^{24}$$

$$8^t = 6.0 \times 10^{24} \cdot 10^{15} = 6.0 \times 10^{39}$$

$$t \ln(8) = \ln(6.0 \times 10^{39})$$

$$t = \ln(6.0 \times 10^{39}) / \ln(8)$$

$$= 44.05$$