

# Mathematics 172

Quiz # 10

Name: Key

*You must show your work to get full credit.*

A small pond has a population of bluegill. Let  $N(t)$  be the number of bluegill after  $t$  years. Due to fishing pressure and predation by bass the intrinsic growth rate of the bluegill population has an intrinsic growth rate of  $r = -0.1$ .

1. What is the rate equation satisfied by  $N(t)$ ? (Note a rate equation is an equation, so it will have an equal sign in it) and have a rate (i.e. derivative) in it.

Rate equation is  $\frac{dN}{dt} = -0.1N$

2. The farmer that owns the pond, decides to stock the pond with bluegill to keep the population from dying out. If she stocks at a rate for  $S$  fish/year what is the new rate equation satisfied by  $N$ ?

New rate equation is  $\frac{dN}{dt} = -0.1N + S$

3. At what rate (that is what is the value of  $S$ ) should the farmer stock the pond to have a stable population of 1,000 bluegill?

$$\text{Set } -0.1N + S = 0$$

$$S = \underline{1000}$$

solve for  $N$

$$N = \frac{S}{0.1}$$

we want this to be 1000

$$\text{so } \frac{S}{0.1} = 1000$$

$$S = (0.1)(1000) = 100$$