

Mathematics 172 Homework

1. Solve the initial value problem for the rate equation

$$P' = -.4(P - 200), \quad P(0) = 180$$

by doing the substitution $y = P - 200$.

Answer: $P(t) = 200 - 20e^{-.4t}$.

2. Solve the initial value problem

$$\frac{dN}{dt} = .3(N - 75), \quad N(0) = 80.$$

Answer: $N(t) = 75 + 5e^{.3t}$.

3. Solve the initial value problem

$$P' = -.2P + 600, \quad P(0) = 2,800.$$

Answer: We have to work on this one a bit to see what substitution to do. Factor out the $-.2$ to get

$$P' = -.2(P - 3,000).$$

So the correct substitution is $y = P - 3,000$. You can now solve and get

$$P = 3,000 - 200e^{-.2t}.$$

4. Solve

$$N' = -.13N + 500 \quad N(0) = 4,000.$$

Answer: $N(t) = 3846.15 + 153.85e^{-.13t}$