

Quiz #2

Name: Key*You must show your work to get full credit.*

1. Assume that  $y = f(x)$  is a function of  $x > 0$  such that when the input,  $x$ , is doubled, then the output,  $y$ , is doubled, and when the input is tripled the output is tripled. Assume that  $f(5) = 16$ .

(a) Find a formula for  $y$  in terms of  $x$ .

$$y = \underline{y = 3.2x}$$

This implies  $y = cx$   
for a constant  $c$ .  
when  $x=5, y=16$  so  
 $16 = 5c$   
 $c = \frac{16}{5} = 3.2$

(b) If  $x = 27$ , what is the value of  $y$ .

$$f(27) = \underline{86.4}$$

$$f(27) = 3.2(27) = 86.4$$

2. If a 5 foot palmetto weighs 45 pounds, estimate the weight of a 15 foot palmetto tree.

Weight is proportional  
to the cube of  
height. so

Estimated weight is 1215 lbs

$$w = ch^3 \quad (w = \text{weight}, h = \text{height})$$

when  $h=5, w=45$

so  $45 = c(5)^3$

$$c = \frac{45}{5^3} = .36$$

$$w = .36 h^3$$

Thus when  $h=15$  we set

$$w = .36(15)^3 = 1215$$