

Homework assigned Wednesday, September 15

Problem 1. *This is a hold over from Monday.* A population of fish in a large tank grows logistically with a carrying capacity of 500, and an intrinsic growth rate of $r = .2$ (fish/month)/fish.

- (a) If internally 300 fish are put into the tank, then what are the initial growth rate of the population and the initial per capita growth rate?
- (b) After some point the fish are harvested at rate of 15% of the population per month. What happens to the size of the stable population?

Problem 2. As in the last problem, a population of fish in a tank grows logistically with a carrying capacity of 500, and an intrinsic growth rate of $r = .2$ (fish/month)/fish. If we now harvest the fish at a of 15 fish/month.

- (a) Explain why the new rate equation is

$$\frac{dN}{dt} = .2N \left(1 - \frac{N}{500} \right) - 15.$$

- (b) Use your calculator to find the equilibrium points of this equation. (There are two of them.)
- (c) Sketch a graph of some solutions to the rate equation.
- (d) What is the new stable population size.
- (e) Is there a threshold so that if the population size drops below this threshold the population dies off.