

1. The growth rate of a population  $P = P(t)$  is governed by the model equation  $\frac{dP}{dt} = 0.04P \left(1 - \frac{P}{80}\right)$ . Determine all the equilibrium values. Sketch the long term behavior of  $P(t)$  given each of the initial conditions.
- $P(0) = 20$ . Label this graph A.
  - $P(0) = 100$ . Label this graph B.
  - $P(0) = 60$ . Label this graph C.
  - Now suppose 0.04 is replaced by 0.01 in the model. Take  $P(0) = 20$  again. Sketch the new graph and label it D.

2. The growth rate of a population  $N = N(t)$  is governed by the model equation  $\frac{dN}{dt} = 0.04N \left(1 - \frac{N}{150}\right) \left(\frac{N}{30} - 1\right)$ . If  $N(0) = 25$ , sketch the long term behavior of  $N(t)$ , and explain why the graph has the shape that it does.