MATH 141 (Section 11 & 12) Prof. Meade

Exam 4 – Practice November 19, 2007 University of South Carolina Fall 2007

Name: \_ Section: 011 / 012 (circle one)

Instructions:

- 1. There are a total of 7 problems on 6 pages. Check that your copy of the exam has all of the problems.
- 2. Calculators may not be used for any portion of this exam.
- 3. You must show all of your work to receive credit for a correct answer.
- 4. Your answers must be written legibly in the space provided. You may use the back of a page for additional space; please indicate clearly when you do so.

	Problem	Points	Score
	1	20	
	2	15	
	3	15	
	4	15	
	5	15	
	6	10	
	7	10	
	Total	100	
Study Smart!			!

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- 1. (20 points) Let  $f(x) = xe^{-x/2}$ . Find
  - (a) the interval(s) on which f is increasing
  - (b) the interval(s) on which f is decreasing
  - (c) the open intervals on which f is concave up
  - (d) the open interval(s) on which f is concave down
  - (e) the x-coordinates of all inflection points

NOTE: Be sure to show your work and to label your answers clearly.

2. (15 points) Let  $f'(x) = \frac{2-3x}{\sqrt[3]{x+2}}$  be the first derivative of a continuous function f. Find all critical points of f and determine whether each is a relative maximum, relative minimum, or neither.

NOTE: Show enough work to justify your answers.

3. (15 points) Sketch the graph of a continuous curve y = f(x) with the following properties: f(2) = 4, f'(2) = 0, f''(x) > 0 for x < 2, f''(x) > 0 for x > 2.

4. (15 points) Find the absolute maximum and absolute minimum values of  $f(x) = \sin(x) - \cos(x)$ on  $[0, \pi]$ .



5. (15 points) Consider the following applied optimization problem:

A closed rectangular container with a square base is to have a volume of  $2000 \text{ cm}^3$ . It costs twice as much per square centimeter for the top and bottom as it does for the sides. Find the dimensions of the container of least cost.

Find

- (a) the function to be maximized or minimized (indicate which it is)
- (b) the interval of possible values for the variable in this problem

Do not solve the optimization problem.

6. (10 points) Determine if the hypotheses of the Mean-Value Theorem are satisfied for  $f(x) = \frac{1}{x-1}$  on the interval [2,5]. If they are, find all values of c in this interval that satisfy the conclusion of the theorem.

7. (10 points) The position function of a particle moving on a horizontal x-axis is shown below.



- (a) Is the particle moving left or right at time a?
- (b) Is the acceleration positive, negative, or zero at time a?
- (c) Is the particle speeding up or slowing down at time a?
- (d) Is the particle speeding up or slowing down at time b?